

# Trigonometry Formulas Sheet

Comprehensive trig formulas from basic ratios to advanced identities. Your complete reference for trigonometry.

## SOH CAH TOA

$\sin(\theta) = \text{opposite} / \text{hypotenuse}$

$\cos(\theta) = \text{adjacent} / \text{hypotenuse}$

$\tan(\theta) = \text{opposite} / \text{adjacent}$

## Reciprocal Functions

$\csc(\theta) = 1 / \sin(\theta) = \text{hyp} / \text{opp}$

$\sec(\theta) = 1 / \cos(\theta) = \text{hyp} / \text{adj}$

$\cot(\theta) = 1 / \tan(\theta) = \text{adj} / \text{opp}$

## Pythagorean Identities

$$\sin^2\theta + \cos^2\theta = 1$$

$$1 + \tan^2\theta = \sec^2\theta$$

$$1 + \cot^2\theta = \csc^2\theta$$

## Unit Circle Key Angles

Degrees	Radians	$\sin(\theta)$	$\cos(\theta)$	$\tan(\theta)$
0	0	0	1	0
30	$\pi/6$	1/2	$\sqrt{3}/2$	1/3
45	$\pi/4$	$\sqrt{2}/2$	$\sqrt{2}/2$	1
60	$\pi/3$	$\sqrt{3}/2$	1/2	$\sqrt{3}$
90	$\pi/2$	1	0	undefined

Memory trick: For sin values at 0, 30, 45, 60, 90 think 0/2, 1/2,  $\sqrt{2}/2$ ,  $\sqrt{3}/2$ , 1/2.

# Trigonometry Formulas (continued)

Double angle, sum/difference formulas, and triangle laws.

## Double Angle Formulas

$$\sin(2\theta) = 2 \sin(\theta) \cos(\theta)$$

$$\cos(2\theta) = \cos^2\theta - \sin^2\theta$$

$$\cos(2\theta) = 2\cos^2\theta - 1$$

$$\cos(2\theta) = 1 - 2\sin^2\theta$$

$$\tan(2\theta) = 2\tan(\theta) / (1 - \tan^2\theta)$$

## Sum and Difference

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\tan(A \pm B) = (\tan A \pm \tan B) / (1 \mp \tan A \tan B)$$

## Law of Sines

$$a / \sin(A) = b / \sin(B) = c / \sin(C)$$

Use when you know two angles and one side, or two sides and a non-included angle.

## Law of Cosines

$$c^2 = a^2 + b^2 - 2ab \cos(C)$$

Use when you know two sides and the included angle, or all three sides.

## Half Angle Formulas

$$\sin(\theta/2) = \pm((1 - \cos\theta) / 2)$$

$$\cos(\theta/2) = \pm((1 + \cos\theta) / 2)$$

$$\tan(\theta/2) = \sin(\theta) / (1 + \cos\theta) = (1 - \cos\theta) / \sin(\theta)$$

For the Law of Cosines, when  $C = 90$  degrees,  $\cos(C) = 0$  and it reduces to the Pythagorean theorem:  $c^2 = a^2 + b^2$ .